Cambridge IGCSE

| CANDIDATE NAME | |
|---|---|

| CENTRE NUMBER | | CANDIDATE NUMBER | |
|---|---|---|---|

**MATHEMATICS** 0580/21

Paper 2 (Extended) May/June 2017

**1 hour 30 minutes**

Candidates answer on the Question Paper.

Additional Materials: Electronic calculator Geometrical instruments
Tracing paper (optional)

**READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name on all the work you hand in.
Write in dark blue or black pen.
You may use an HB pencil for any diagrams or graphs.
Do not use staples, paper clips, glue or correction fluid.
DO **NOT** WRITE IN ANY BARCODES.

Answer **all** questions.
If working is needed for any question it must be shown below that question.
Electronic calculators should be used.
If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.
For π, use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.
The number of marks is given in brackets [ ] at the end of each question or part question.
The total of the marks for this paper is 70.

CAMBRIDGE International Examinations

**[Turn over**

**1** Simplify.
$$(x^2)^5$$

.............................................. [1]

**2** The thickness of one sheet of paper is $8 \times 10^{-3}$ cm.

Work out the thickness of 250 sheets of paper.

........................................ cm [1]

**3** Write 23.4571 correct to

**(a)** 4 significant figures,

.............................................. [1]

**(b)** the nearest 10.

.............................................. [1]

**4** The table shows the temperatures in five places at 10 am one day in January.

| Place | Temperature (°C) |
|---------|------------------|
| Helsinki | −7 |
| Chicago | −10 |
| London | 3 |
| Moscow | −4 |
| Bangkok | 26 |

**(a)** Which place was the coldest?

.............................................. [1]

**(b)** At 2 pm the temperature in Helsinki had increased by 4 °C.

Write down the temperature in Helsinki at 2 pm.

........................................ °C [1]

**5** Factorise completely.
$$12n^2 - 4mn$$

.............................................. [2]

**6** **(a)** $2^r = \dfrac{1}{16}$

Find the value of $r$.

$r = $ ....................................... [1]

**(b)** $3^t = \sqrt[5]{3}$

Find the value of $t$.

$t = $ ....................................... [1]

**7** **Without using a calculator**, work out $1\dfrac{2}{3} + \dfrac{5}{7}$.

Write down all the steps of your working and give your answer as a mixed number in its simplest form.

.............................................. [3]

**8** Simon has two boxes of cards.
In one box, each card has one shape drawn on it that is either a triangle or a square.
In the other box, each card is coloured either red or blue.

Simon picks a card from each box at random.
The probability of picking a triangle card is $t$.
The probability of picking a red card is $r$.

Complete the table for the cards that Simon picks, writing each probability in terms of $r$ and $t$.

| Event | Probability |
|---|---|
| Triangle and red | |
| Square and red | $(1-t)\,r$ |
| Triangle and blue | |
| Square and blue | |

[3]

**9** $h$ is directly proportional to the square root of $p$.
$h = 5.4$ when $p = 1.44$ .

Find $h$ when $p = 2.89$ .

$h =$ ...................................... [3]

**10**
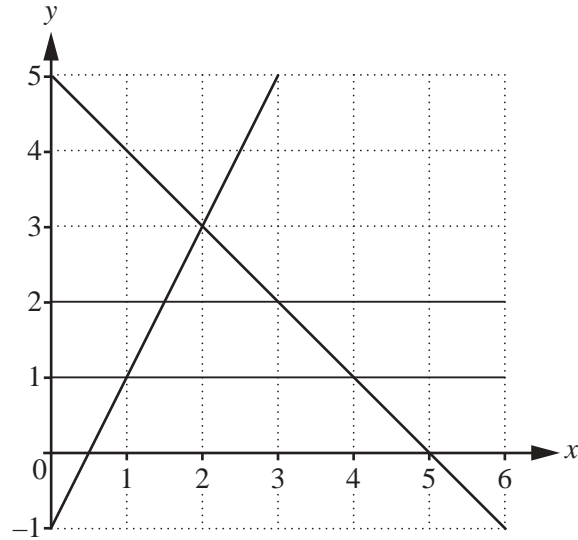


By shading the **unwanted** regions of the grid, find and label the region *R* that satisfies the following four inequalities.

$$y \leqslant 2 \qquad y \geqslant 1 \qquad y \leqslant 2x - 1 \qquad y \leqslant 5 - x \qquad \text{[3]}$$

**11** The two barrels in the diagram are mathematically similar.



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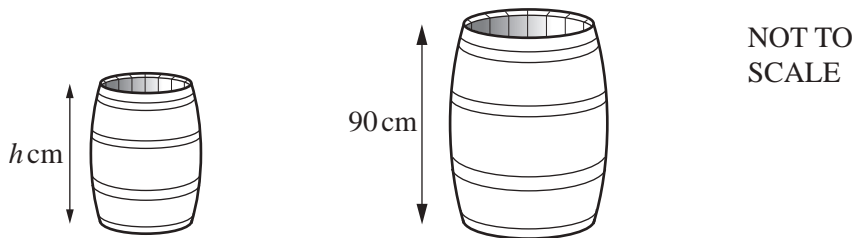
The smaller barrel has a height of *h* cm and a capacity of 100 litres.
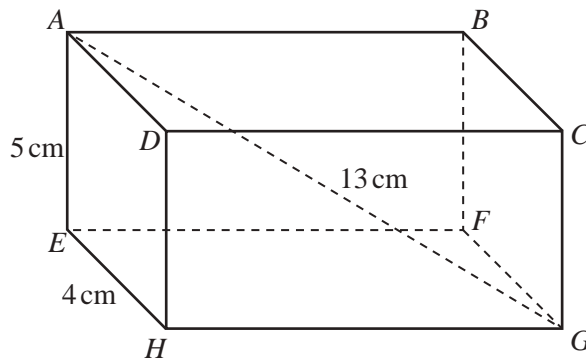The larger barrel has a height of 90 cm and a capacity of 160 litres.

Work out the value of *h*.

*h* = ...................................... [3]

 **[Turn over**

**12** A line has gradient 5.
M and N are two points on this line.
M is the point (x, 8) and N is the point (k, 23).

Find an expression for x in terms of k.
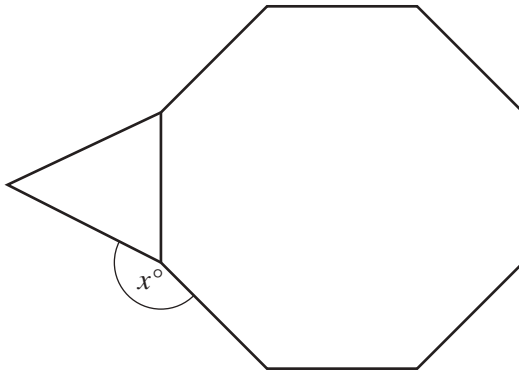
$x =$ ...................................... [3]

**13**



The diagram shows a cuboid ABCDEFGH.
AE = 5 cm, EH = 4 cm and AG = 13 cm.

Calculate the angle between the line AG and the base EFGH of the cuboid.

.............................................. [3]

**14** The diagram shows a regular octagon joined to an equilateral triangle.

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Work out the value of *x*.

*x* = ...................................... [3]

**15** The diagram shows information about the first 100 seconds of a car journey.
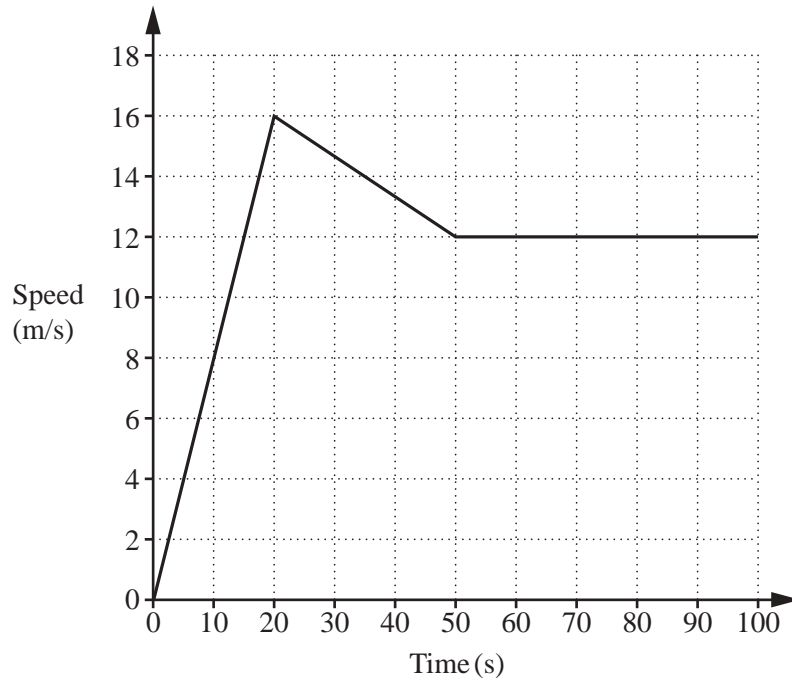


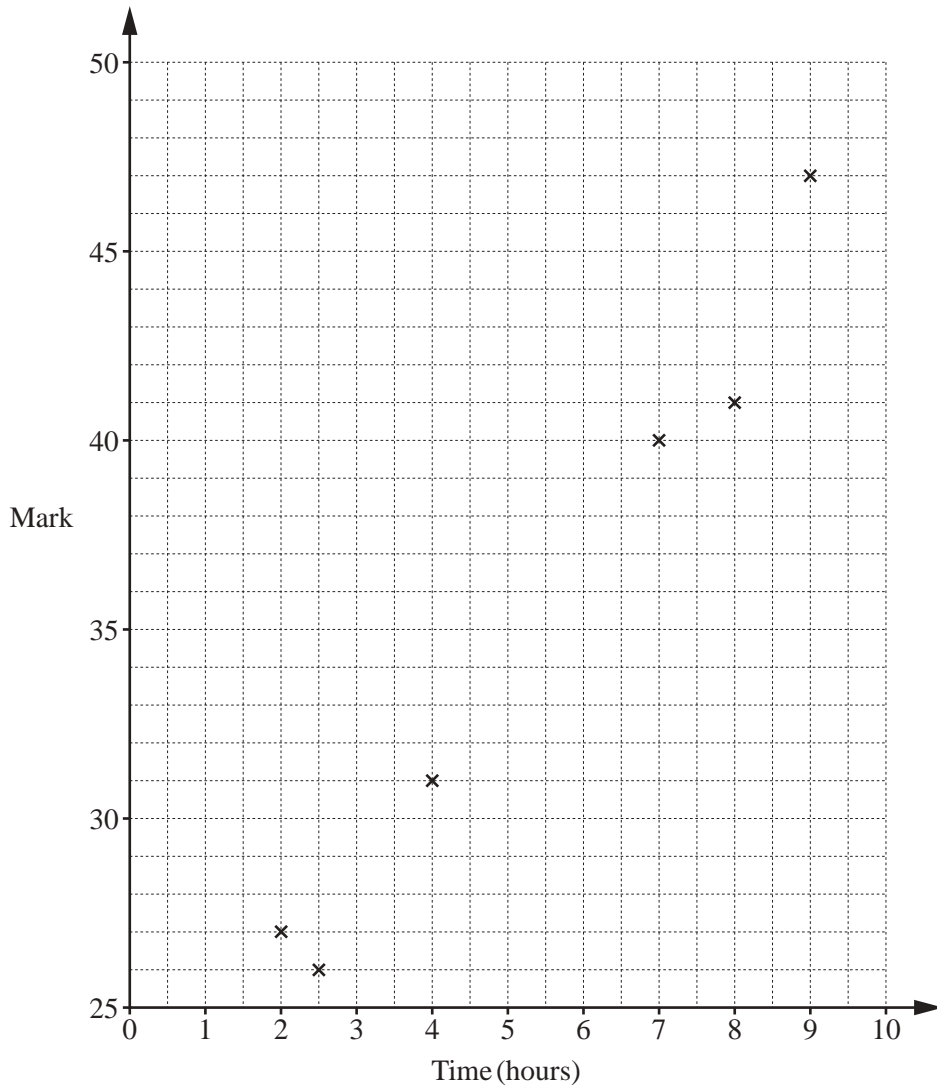**(a)** Calculate the acceleration during the first 20 seconds of the journey.

....................................m/s$^2$ [1]

**(b)** Work out the total distance travelled by the car in the 100 seconds.

..........................................m [3]

**16** Six students revise for a test.
The scatter diagram shows the time, in hours, each student spent revising and their mark in the test.



**(a)** The data for two more students is shown in the table.

| Time (hours) | 4.5 | 6.5 |
|---|---|---|
| Mark | 33 | 35 |

Plot these two points on the scatter diagram. [1]

**(b)** What type of correlation is shown on the scatter diagram?

.............................................. [1]

**(c)** Draw a line of best fit on the scatter diagram. [1]

**(d)** Another student spent 5.5 hours revising.
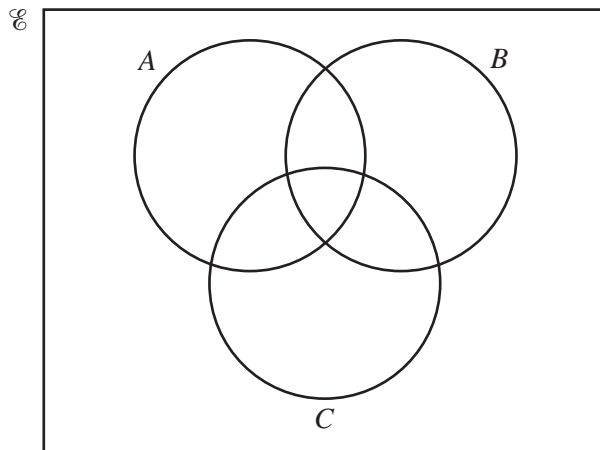
Estimate a mark for this student.

.............................................. [1]

**17 (a)** In this Venn diagram, shade the region $F \cup G'$.



[1]
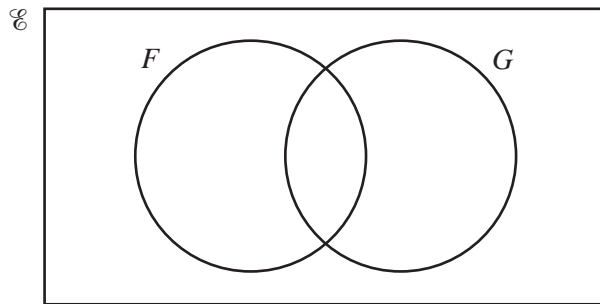
**(b)** $\mathscr{E} = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$
$A = \{x: x \text{ is an odd number}\}$
$B = \{x: x \text{ is a square number}\}$
$C = \{x: x \text{ is a multiple of 3}\}$

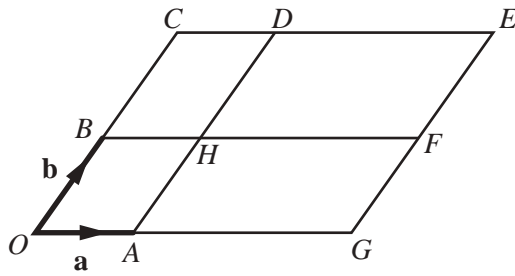**(i)** Write all the elements of $\mathscr{E}$ in the Venn diagram below.



[2]

**(ii)** Another number is included in the set $\mathscr{E}$.
This number is in the region $A' \cap B \cap C$.

Write down a possible value for this number.

................................................ [1]

**18** The diagram shows a parallelogram *OCEG*.



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*O* is the origin, $\overrightarrow{OA} = \mathbf{a}$ and $\overrightarrow{OB} = \mathbf{b}$.
*BHF* and *AHD* are straight lines parallel to the sides of the parallelogram.
$\overrightarrow{OG} = 3\overrightarrow{OA}$ and $\overrightarrow{OC} = 2\overrightarrow{OB}$.

**(a)** Write the vector $\overrightarrow{HE}$ in terms of **a** and **b**.

$\overrightarrow{HE} =$ .................................. [1]

**(b)** Complete this statement.

**a** + 2**b** is the position vector of point ......................... [1]

**(c)** Write down two vectors that can be written as 3**a** − **b**.

............................... and ............................... [2]

**19** *ABCD* is a rhombus with side length 10 cm.
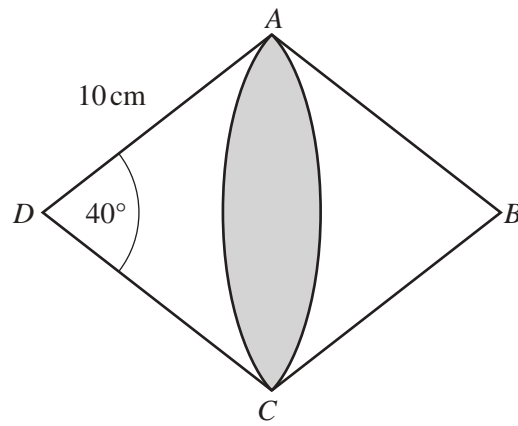


Angle *ADC* = 40°.
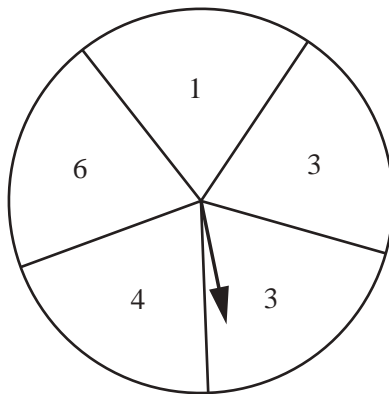*DAC* is a sector of a circle with centre *D*.
*BAC* is a sector of a circle with centre *B*.

Calculate the shaded area.

..................................... cm² [4]

**20** The diagram shows a fair spinner.



Anna spins it twice and adds the scores.

**(a)** Complete the table for the total scores.

| | | Score on first spin | | | | |
|---|---|---|---|---|---|---|
| | | 1 | 3 | 3 | 4 | 6 |
| Score on second spin | 1 | 2 | 4 | 4 | 5 | 7 |
| | 3 | 4 | 6 | 6 | 7 | 9 |
| | 3 | 4 | 6 | 6 | 7 | 9 |
| | 4 | | | | | |
| | 6 | | | | | |

[1]

**(b)** Write down the most likely total score.

................................................ [1]

**(c)** Find the probability that Anna scores

  **(i)** a total less than 6,

................................................ [2]

  **(ii)** a total of 3.

................................................ [1]
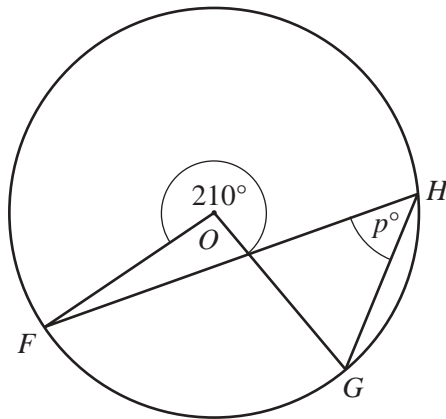
**21 (a)**
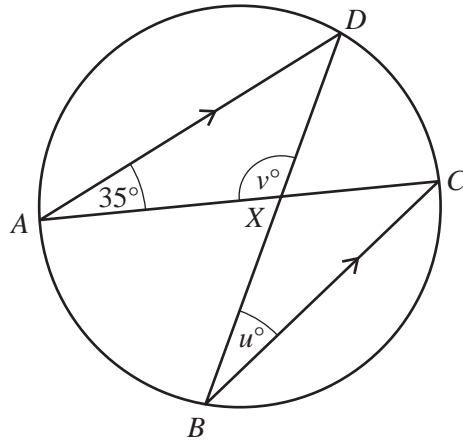


NOT TO SCALE

*A*, *B*, *C* and *D* are points on the circle.
*AD* is parallel to *BC*.
The chords *AC* and *BD* intersect at *X*.

Find the value of *u* and the value of *v*.

*u* = .......................................

*v* = ....................................... [3]

**(b)**



NOT TO SCALE

*F*, *G* and *H* are points on the circle, centre *O*.

Find the value of *p*.

*p* = ....................................... [2]

**22** Write as a single fraction in its simplest form.

**(a)** $\dfrac{x^2 - 3x}{x^2 - 9}$

.............................................. [3]

**(b)** $\dfrac{3}{x-4} + \dfrac{2}{2x+5}$

.............................................. [3]

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